





On the Minimum Induced Drag of Wings

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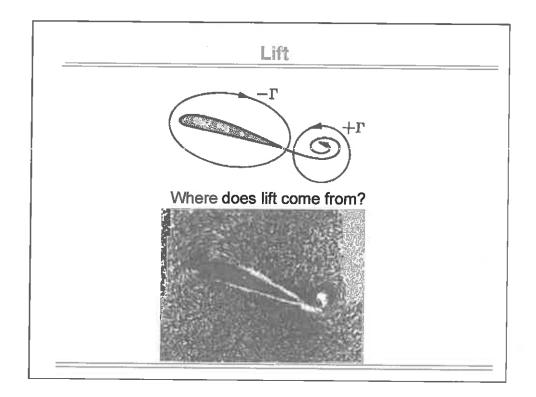
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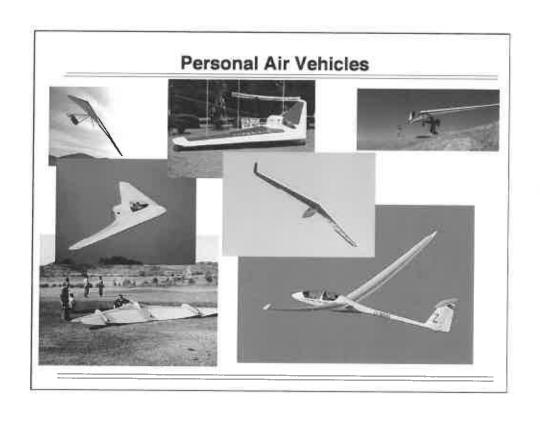
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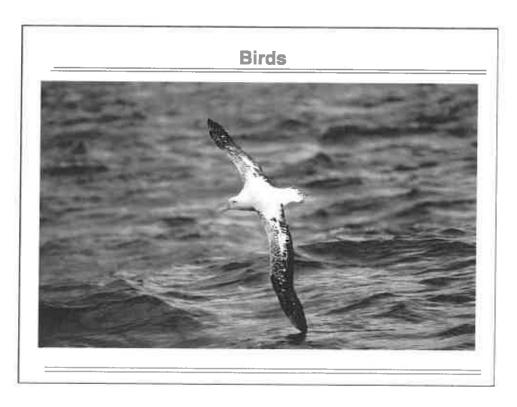


Imagination vs Knowledge

- Requirements and Assumptions
- Concepts and Solutions



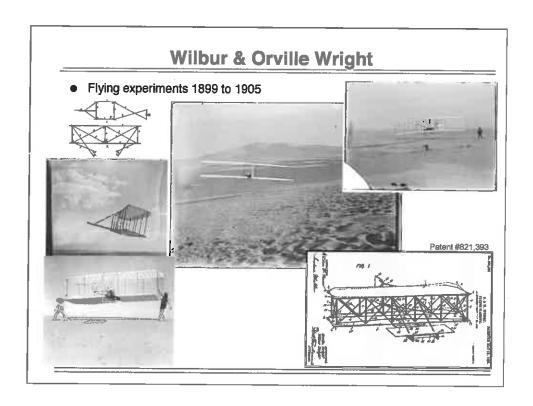




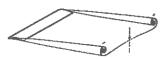
The Four Ways Birds Differ from Aircraft



- Birds turn and maneuver without a vertical tail
- Birds have slender tips that carry little load
- Birds gracefully fly formation with overlapped wingtips
- Birds have narrow wingtips without tip stall



Prandtl Lifting Line Theory



Prandtl's "vortex ribbons"



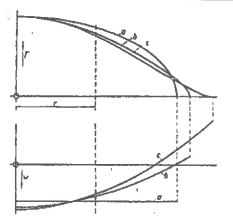
- Elliptical spanload for a given span (1920)
- "the downwash produced by the longitudinal vortices must be uniform at all points on the aerofoils in order that there may be a minimum of drag for a given total lift." y = c



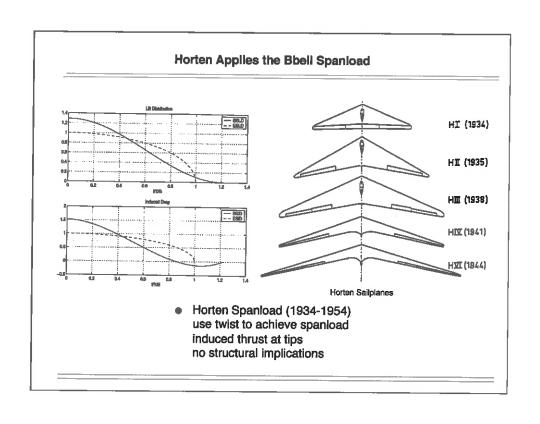
Ludwig Prandtl

This is the accepted theory and the standard for the minimum drag of wings. But what is a wing? Is it only aerodynamic? What about the structure?

Minimum Induced Drag & Bending Moment



Prandtl (1932)
 Constrain minimum induced drag
 Constrain integrated wing bending moment
 22% increase in span with 11% decrease in induced drag

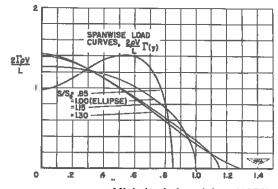




Prandtl & Horten



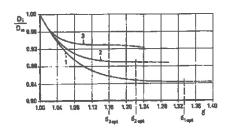
Jones Spanload





- Minimize induced drag (1950)
 Constrain wing root bending moment
 30% increase in span with 17% decrease in induced drag
- "Hence, for a minimum induced drag with a given total lift and a given bending moment the downwash must show a linear variation along the span." y = bx + c

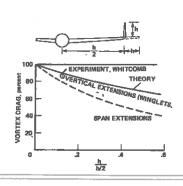
Klein and Viswanathan

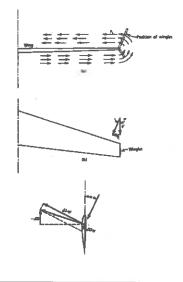


- Minimize induced drag (1975) Constrain bending moment Constrain shear stress 16% increase in span with 7% decrease in induced drag
- "Hence the required downwash-distribution is parabolic." $y = ax^2 + bx + c$

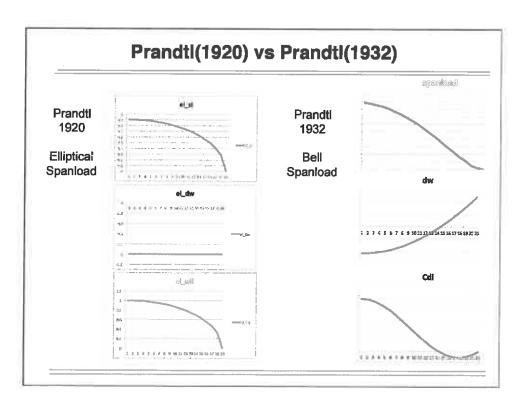
Winglets

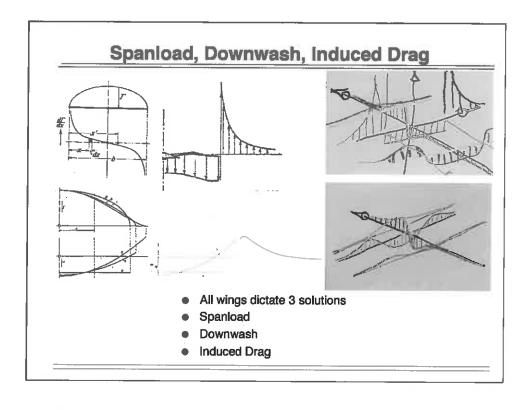
- Richard Whitcomb's Winglets
 induced thrust on wingtips
 induced drag decrease is about half of the span "extension"
 - reduced wing root bending stress





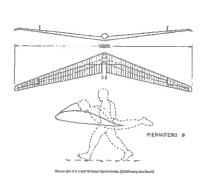


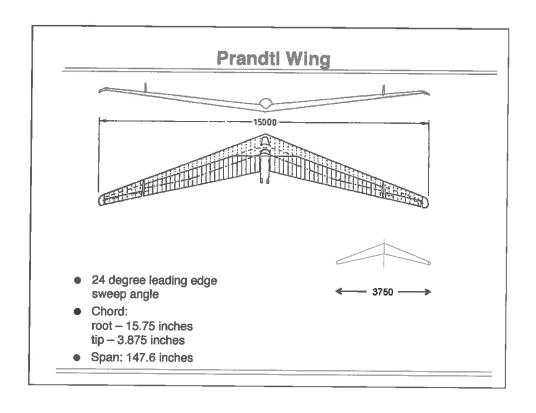


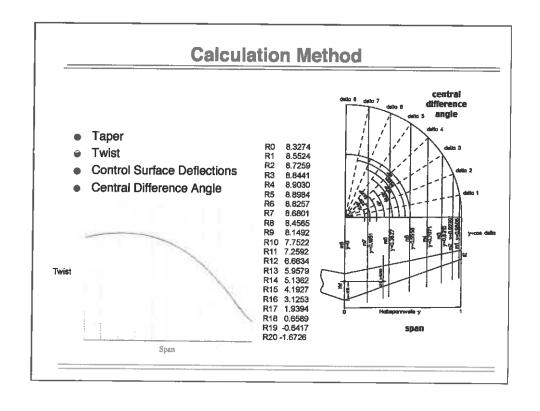


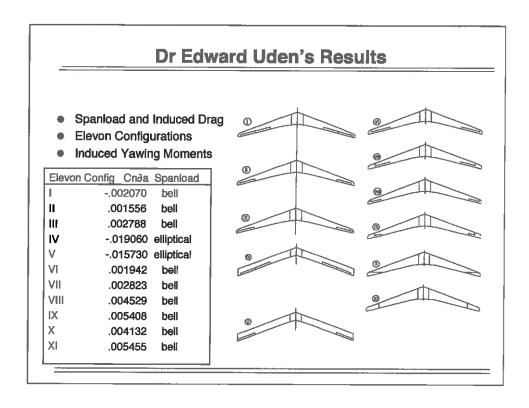
Horten H Xc Example

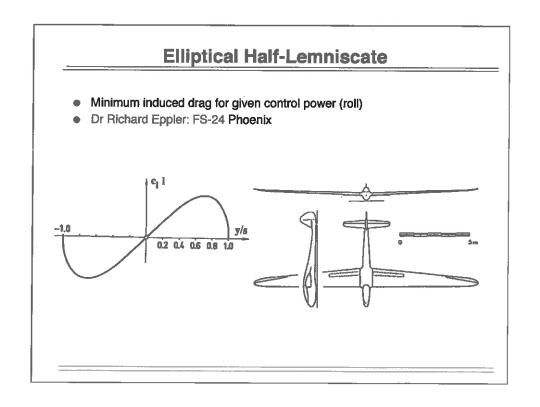
- Horten H Xc footlaunched ultralight sailplane 1950
- 24 degree leading edge sweep angle
- Chord: root - 63 inches tip – 15.75 inches
- Span: 49.2 feet





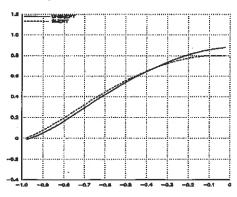


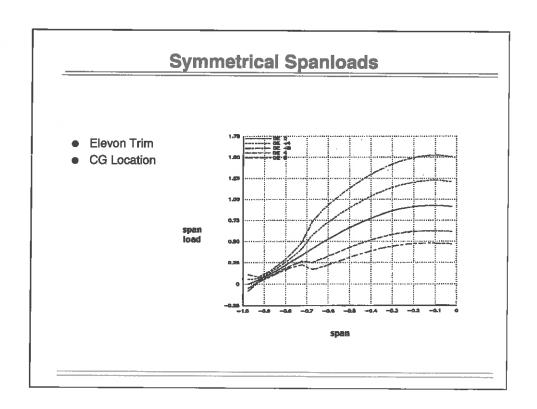




"Mitteleffekt"

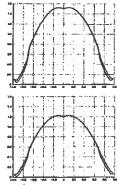
- Artifact of spanload approximations
- Effect on spanloads increased load at tips decreased load near centerline
- Upwash due to sweep unaccounted for

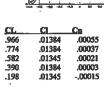


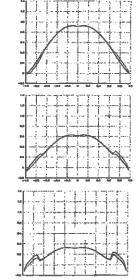


Asymmetrical Spanloads

- Cl∂a (roll due to aileron)
- Cnaa (yaw due to aileron) induced component profile component change with lift
- Cn∂a/Cl∂a
- CL(Lift Coefficient)
 Increased lift:
 increased Cηβ*
 Decreased lift:
 decreased CIβ
 decreased CIβ
 decreased CIβ
 decreased Cηβ*



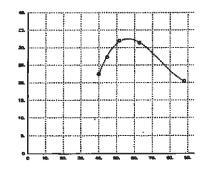




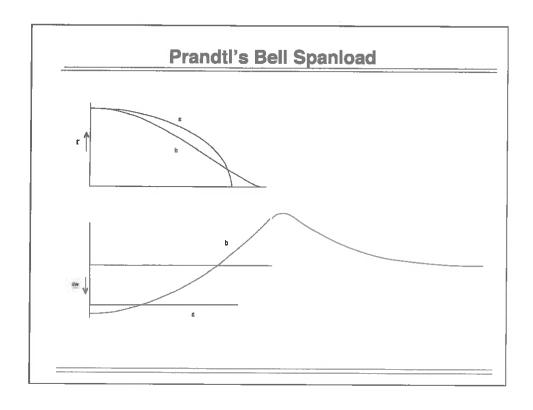
Performance Comparison

L/D

- Max L/D: 31.9
- Min sink: 89.1 fpm
- Does not include pilot drag
- Prediicted L/D: 30
- Predicted sink: 90 fpm



velocity

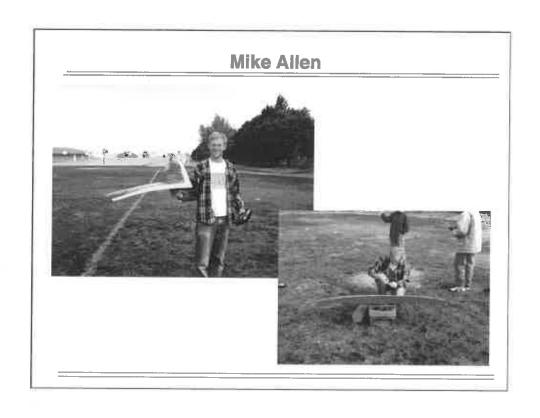


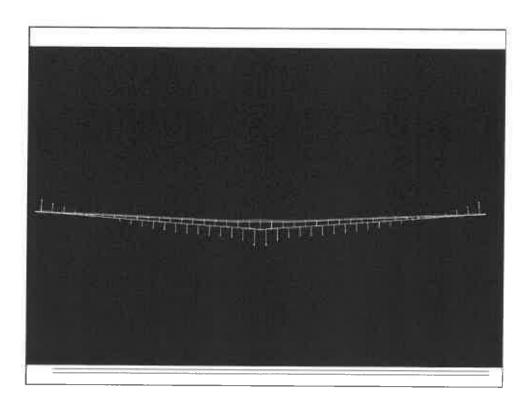


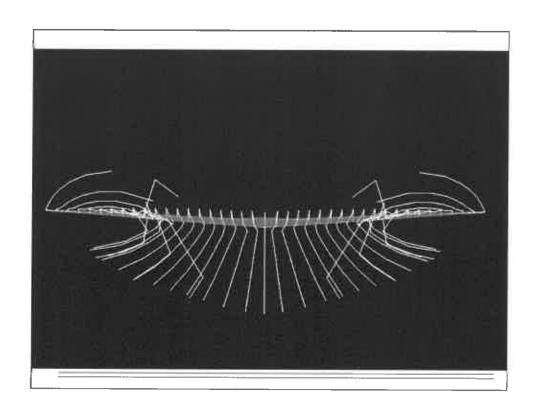
$$\lim_{\mathbf{x}:\ \mathbf{0}\ \rightarrow\ \mathbf{b/2}} \mathsf{L}(\mathbf{x}) \simeq \mathbf{0} \tag{1}$$

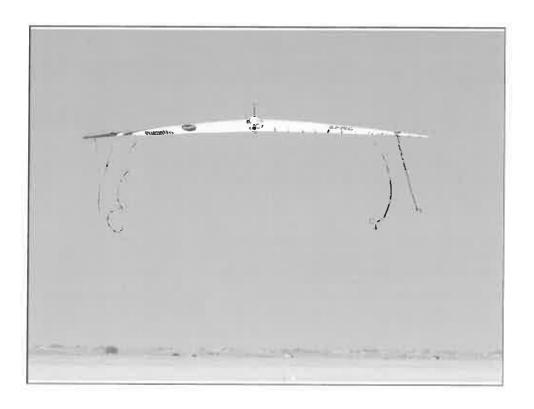
$$\lim_{x: 0 \to b/2} \frac{dL(x)}{dx} = 0$$
 (2)

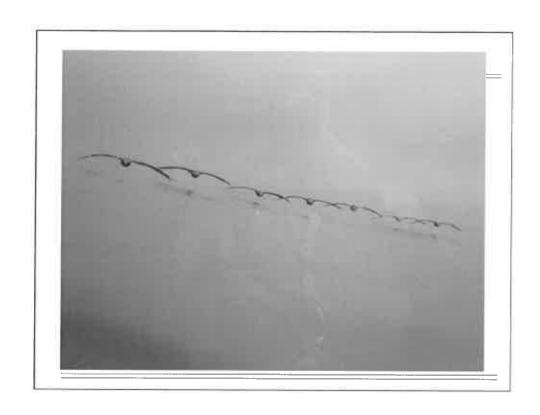
$$\lim_{x:0\to b/2} \frac{d DW(x)}{dx} = \lim_{x:\infty\to b/2} \frac{d DW(x)}{dx}$$
 (3)

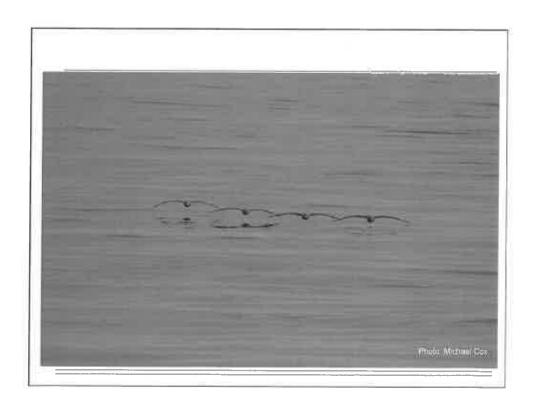










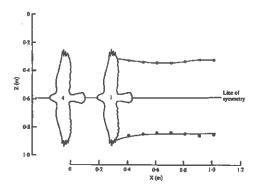


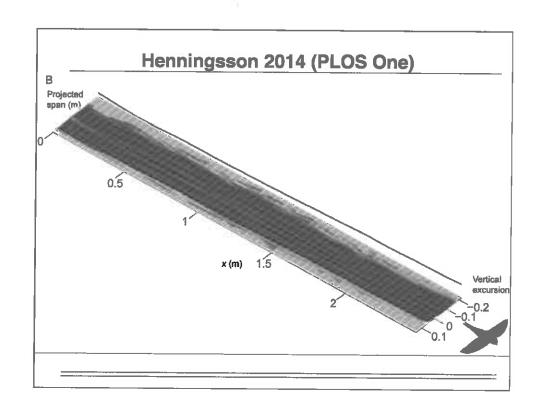
Spanload

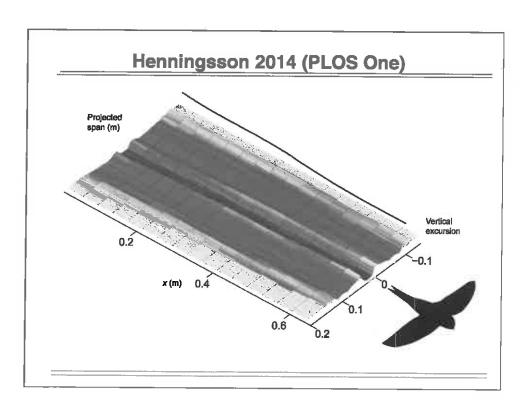


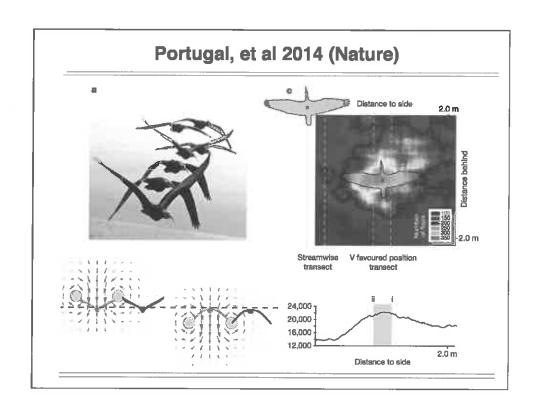
Spedding's Gliding Falcon

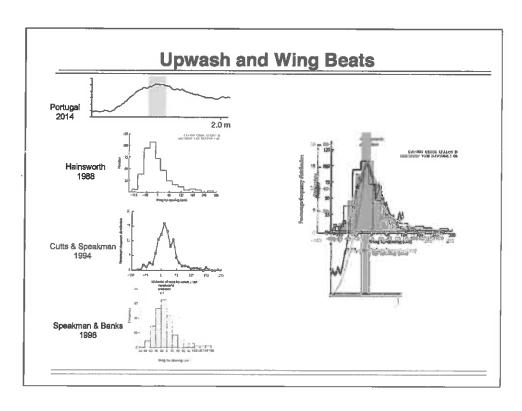
- Spedding photograpgh's a gliding falcon's wake with He bubbles
- Vortex cores are 0.76 b apart
- Elliptical spanload is assumed, so the vortex cores are assumed to come from the wingtips

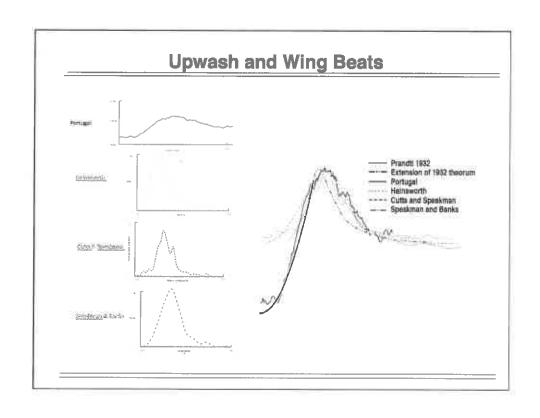


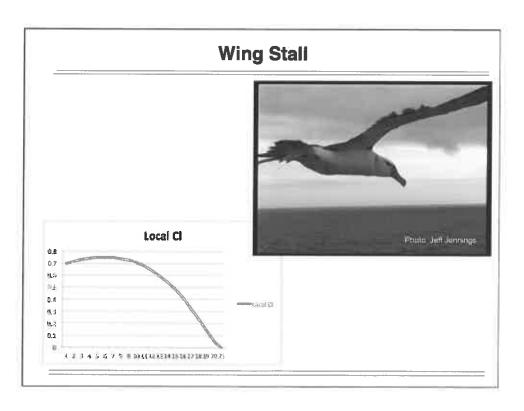


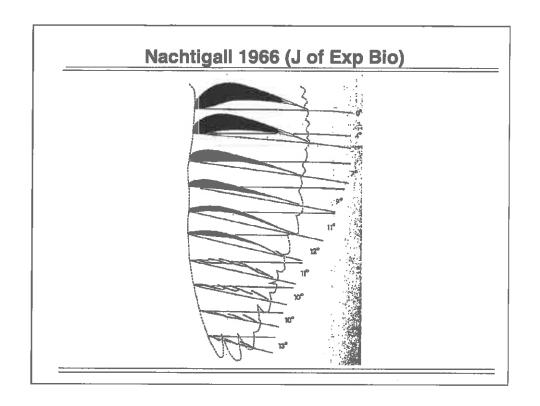


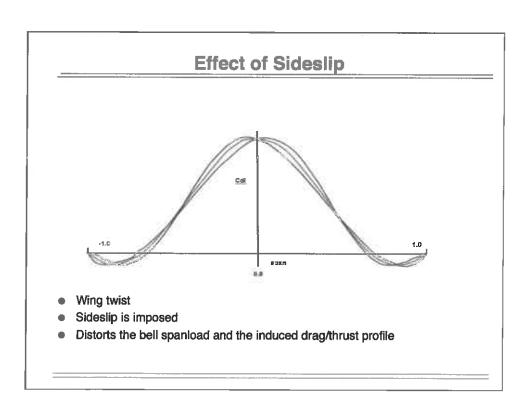


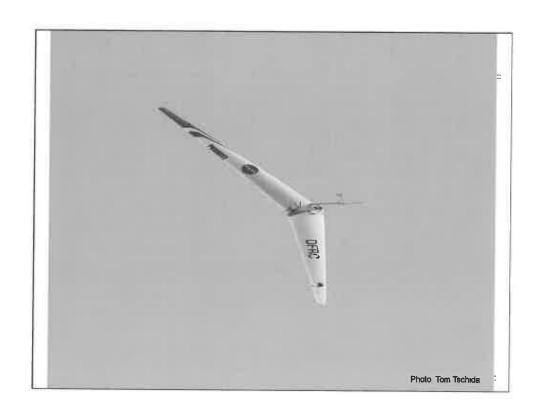


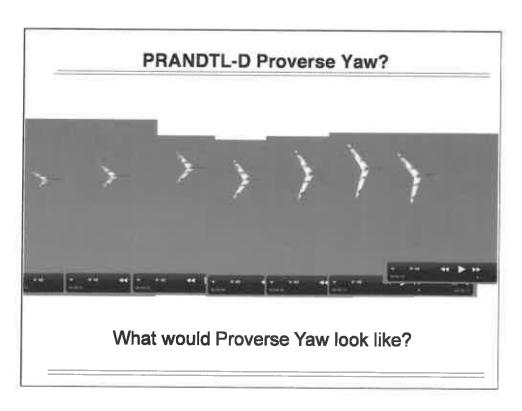






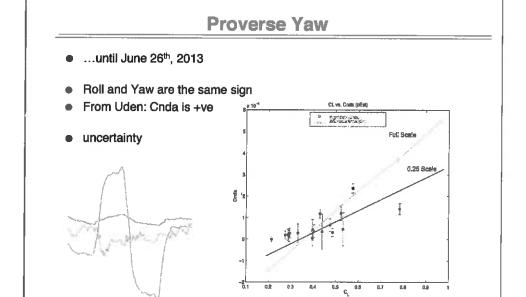




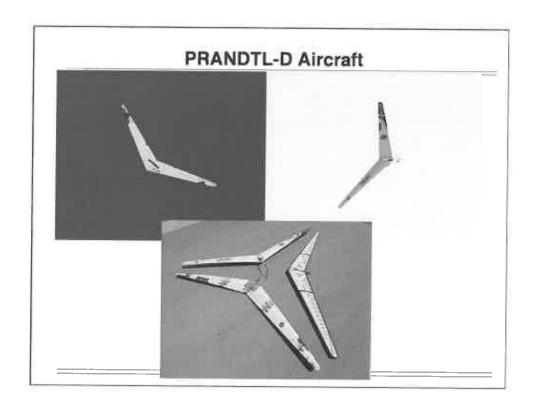


Flight Data

- Measurement of proverse yaw would be the final hurdle to achieve
- Icing on the cake: measure Cnda (yawing moment due to aileron deflection)
- NOT ONE SECOND OF FLIGHT DATA EXISTS TO PROVE ANY OF THIS IS TRUE



Inertias; configuration changes, turbulence, and slope of Cnda





- You Have Three Choices:
- 1/ drag a vertical tail around with you all the time to create a yawing moment
- 2/ manipulate drag at the wing tips to control yaw

-OR-

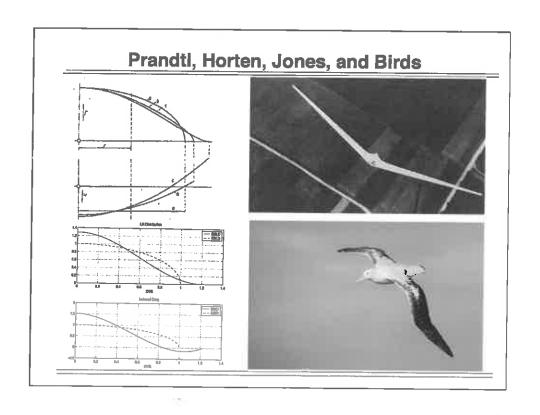
- · 3/ manipulate THRUST at the wing tips to control yaw
- Biological vs Mechanical Flight







Mechanical Flight (110 yrs) Vertabrate Flight (128 My)



Efficiency

- Efficiency: 12.5% increase in wing efficiency
- 20-30% increase in efficiency by eliminating the tail
- 15.4% increase in propulsive efficiency
- TOTAL EFFICIENCY INCREASE: 69%
- CY2011: world jet fuel consumption \$134B
- \$55B in jet fuel saved
- CY2011 World GDP: \$69.7T
- World power production: \$12.0T
- \$1.85T savings in world power production

Concluding Remarks

- Birds as as the first model for flight
- Applied approach gave immediate solutions, departure from bird flight
- Eventual meeting of theory and applications (applied theory)
- Spanload evolution (Prandtl/Horten/Jones/Klein/Viswanathan/Whitcomb/Bowers)
- Solve performance, structure and control with ONE spanload solution!
- 12.5% increase in L/D, ~2% increase in prop efficiency, 20-30% decrease in drag eliminating the tail, ~43-62% reduction in total aero efficiency
- Assumptions and Solutions
- The Wrights disintegrated the flight of birds, and Prandtl/Horten/Jones reintegrated the flight of birds...
- Thanks: Red Jensen, Brian Eslinger, Dr Christian Gelzer, Dr Oscar Murillo, Hayley Foster & Steve Craft, Dr Bob Liebeck, Nalin Ratnayake, Mike Allen, Walter Horten, Georgy Dez-Falvy, Rudi Opitz, Bruce Carmichael, R.T. Jones, Russ Lee, Bob Hoey, Phil Barnes, Dan & Jan Armstrong, Dr Phil Burgers, Ed Lockhart, Andy Kesckes, Dr Paul MacCready, Reinhold Stadler, Dr Edward Uden, & Dr Karl Nickel

NASA Aero Academies & Others

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- 2013 NASA Aero Academy
 - Eric Gutierrez, Louis Edelman, Kristyn Kadala, Nancy Pinon, Cody Karcher, Andy Putch, Hovig Yaralian, Jacob Hall
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If you want to build a ship, don't drum up people to collect wood and don't assign them tasks and work, but rather teach them to long for the endless immensity of the sea...

- Antoine de Saint-Exupery





Questions?

